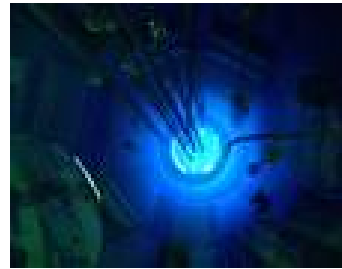


Expanding BEC against defect



Cerenkov light

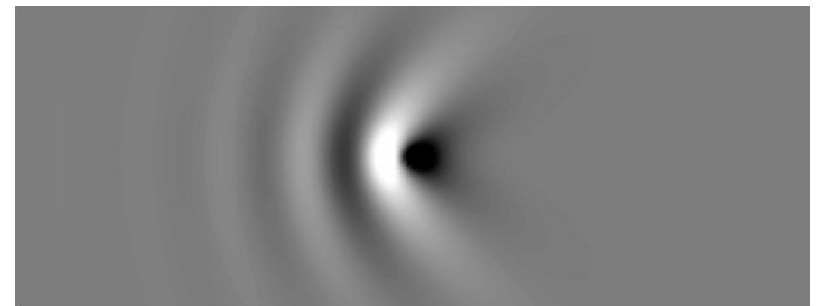


Jet breaking sound barrier

## What do these effects have in common ?



Duck swimming on quiet lake



Real space Rayleigh scattering in solids

# The Cerenkov effect revisited: from swimming ducks to Bose-Einstein condensates

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G. C. La Rocca, F. Bassani (SNS-Pisa), M. Artoni (UniBS, LENS-FI)

C. Ciuti (LPA-ENS, now Univ. Paris 7)

M. Wouters (Univ. Antwerp, Belgium. Now at EPFL)

S.X. Hu, L. A. Collins (LANL)

**Experimental data on atomic BECs:** E. Cornell, P. Engels (JILA)

# What is the Cerenkov effect ??

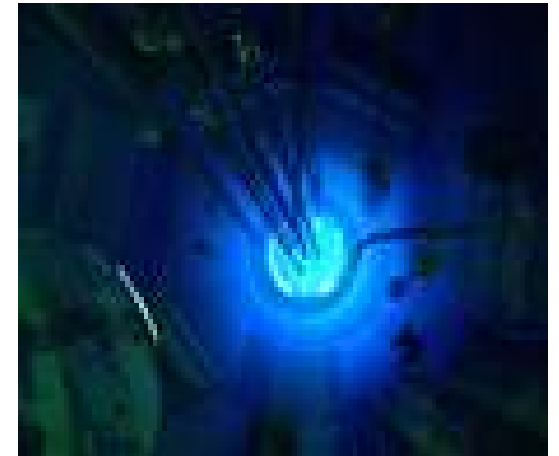
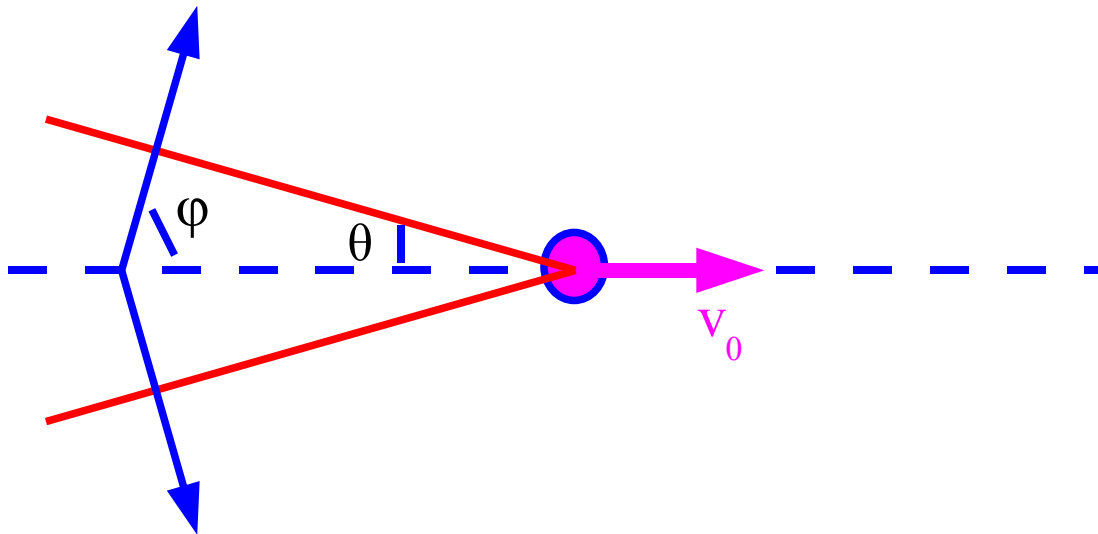
**Charged particle** uniformly moving at (relativistic) speed  $v_0$

**Non-dispersive medium** of refraction index  $n$ , **phase velocity**  $v_{ph} = c / n$

If  $v_0 > v_{ph}$  : light emitted by **Cerenkov effect**

**Radiation** emitted at angle:  $\cos \varphi = v_{ph} / v_0$

**Conical wavefront** of aperture:  $\sin \theta = v_{ph} / v_0$

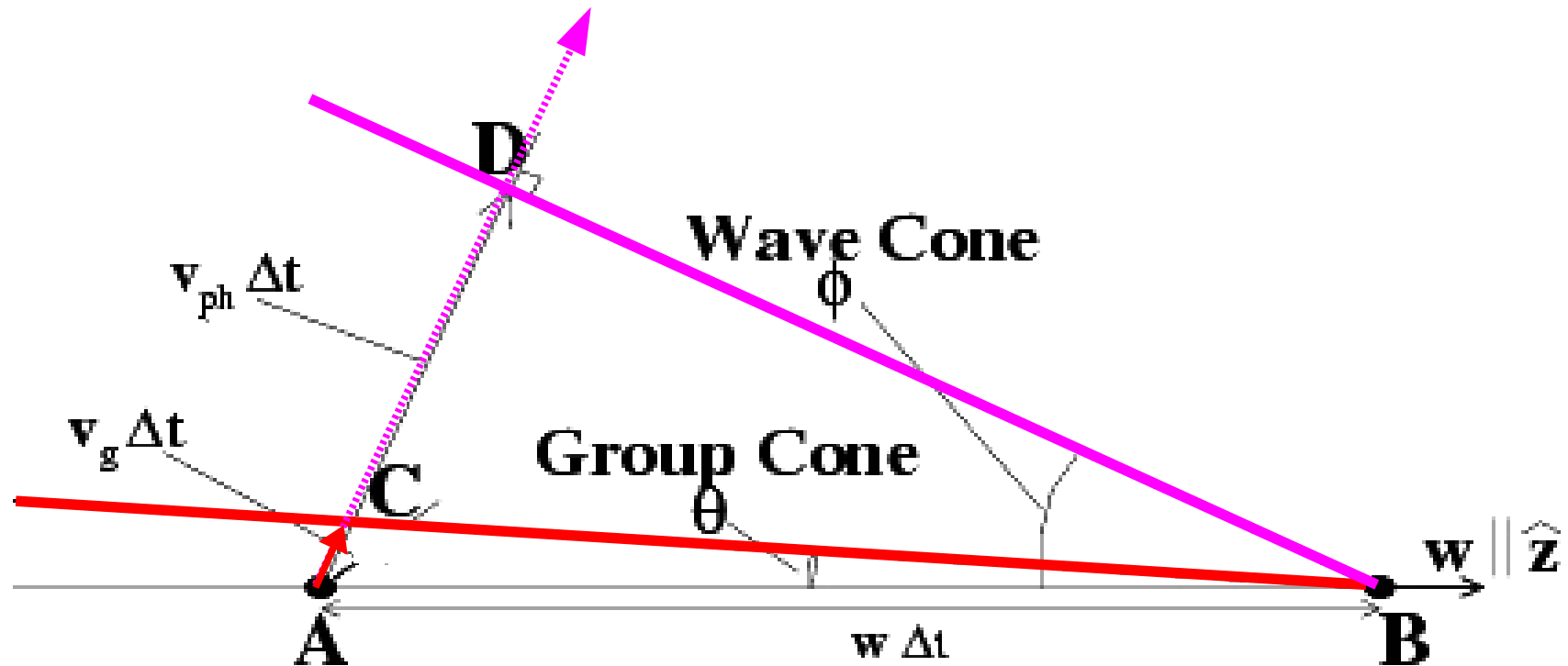


# How I got interested in Cerenkov stuff (a long ago...)

Threshold speed: phase velocity  $v_c = \min_k [\omega(k) / k]$

- What is role of group velocity  $v_{gr}$  in Cerenkov emission ?
- What happens in strongly dispersive, slow-light media  
in which  $v_{gr} \ll v_c$  ?

# Cerenkov emission in slow light media



- (usual) **wave cone**  $\cos \phi = v_{ph} / v$  fixes far-field angle of emission
- **group cone**  $\cos \theta = v_{gr} / v$  fixes spatial region where E field is peaked

I. M. Frank, Nucl. Instr. Meth. A **248**, 7 (1986)

I. Carusotto, M. Artoni, G. C. La Rocca, F. Bassani, PRL **87**, 064801 (2001)

# Many years later...

## Atomic Bose-Einstein condensate

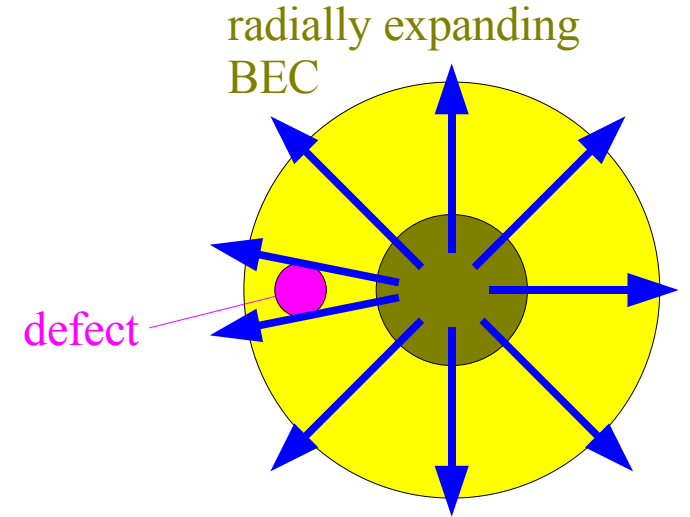
- Harmonic trap suddenly inverted
- BEC expands
- Defect: blue-detuned laser beam
- Wave pattern created in density profile

## As time goes on:

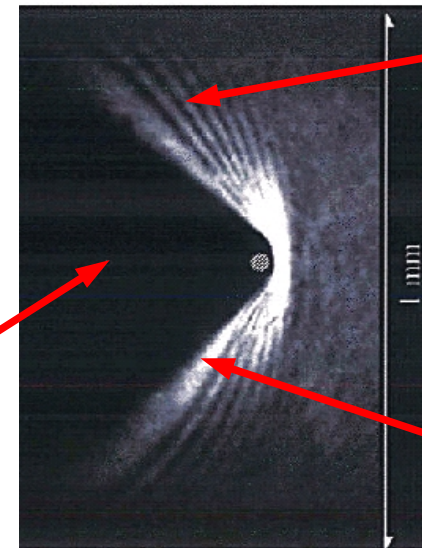
- local velocity  $v_0$  at defect position increases
- local density (and speed of sound  $c_s$ ) decreases

## After different expansion times $t$ :

- different Mach numbers  $M=v/c_s$  probed
- absorptive images



geometrical shadow



wavy precursors

conical wavefront

Experimental picture taken at JILA  
courtesy E. Cornell and P. Engels

# Brute force 3D GPE simulations

Different:

- expansion time  $t$
- defect size  $w$

Longer  $t \rightarrow$  higher speed

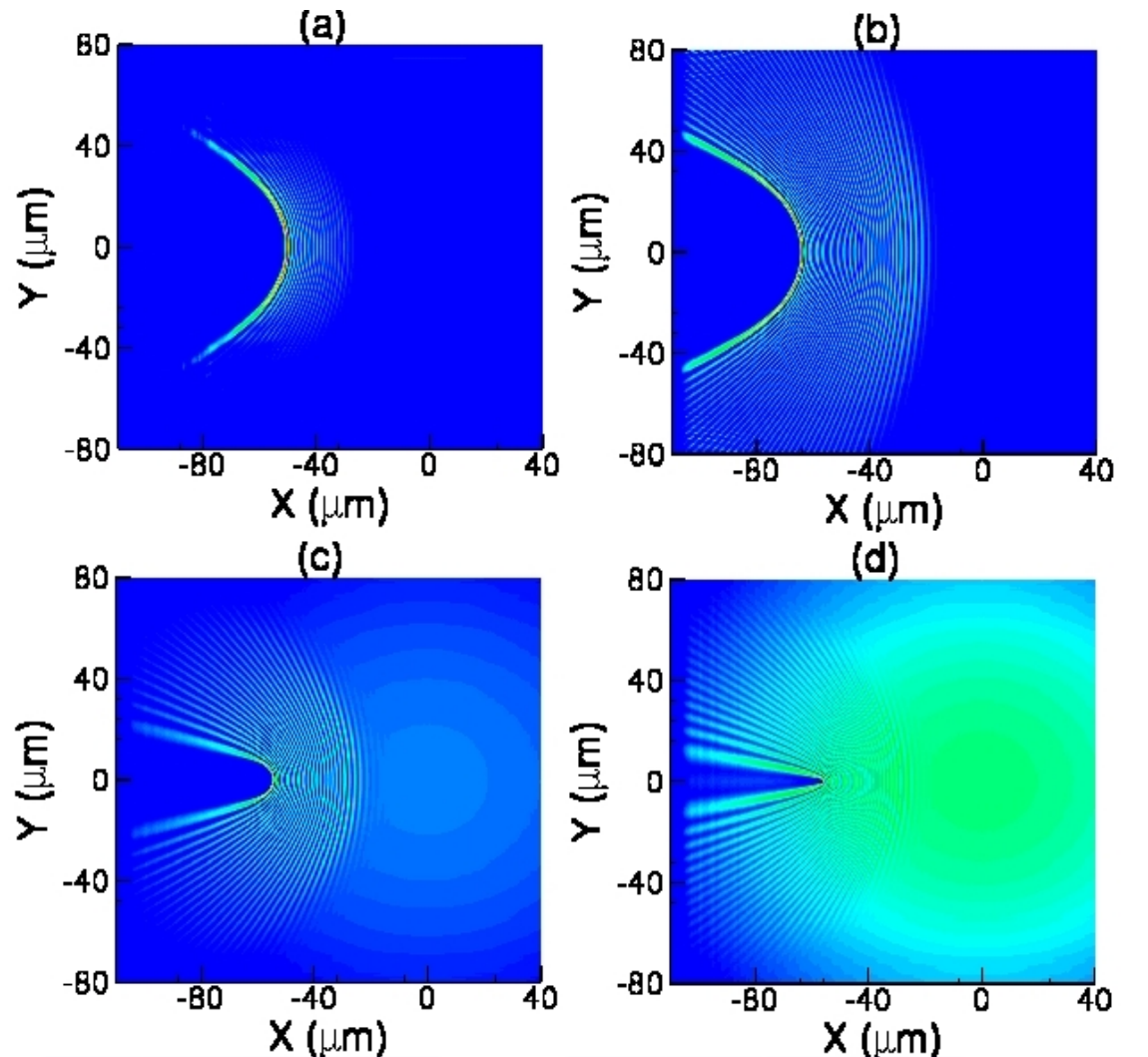
a)  $t=33.6$  ms,  $w=17$  mm

b)  $t=50$  ms,  $w=17$  mm

Smaller defect  $\rightarrow$  narrower shadow

c)  $t=38.4$  ms,  $w=3.74$  mm

d)  $t=38.4$  ms,  $w=0.374$  mm



Good agreement with experiment, but not much physical insight !!

# Theory of Bogoliubov-Cerenkov radiation

Uniform BEC flowing at constant speed  $v$ . BEC wavevector  $\mathbf{k}_0 = m \mathbf{v} / \hbar$

Weak stationary defect potential: Bogoliubov linear response

$$i\hbar \frac{\partial}{\partial t} \delta\vec{\psi} = \mathcal{L} \cdot \delta\vec{\psi} + \vec{F}_d \quad \longrightarrow \quad \delta\vec{\psi}_d = -(\mathcal{L} - i0^+ \mathbf{1})^{-1} \cdot \vec{F}_d$$

Eigenvalues of  $L$ : dispersion of Bogoliubov excitations in moving BEC  
as compared to fluid at rest: additional tilting term  $\mathbf{v} \cdot (\mathbf{k} - \mathbf{k}_0)$

$$\omega(\mathbf{k}) = \mathbf{v} \cdot (\mathbf{k} - \mathbf{k}_0) \pm \sqrt{\frac{\hbar(\mathbf{k} - \mathbf{k}_0)^2}{2m} \left( \frac{\hbar(\mathbf{k} - \mathbf{k}_0)^2}{2m} + 2g\rho_0 \right)}$$

- In defect rest frame, system time-invariant: excitation resonant for  $\mathbf{k}$  modes such that  $\omega(\mathbf{k}) = 0$
- In BEC rest frame standard Cerenkov condition  $\omega_0(\mathbf{k}) - (\mathbf{k} - \mathbf{k}_0) \cdot \mathbf{v} = 0$  recovered !

IC and C.Ciuti, PRL 93, 166401 (2004)

I.Carusotto, S.X.Xu, L.A. Collins, and A. Smerzi, Phys. Rev. Lett. 97, 260403 (2006)



# Theory of Bogoliubov-Cerenkov radiation (II)

## k-space pattern

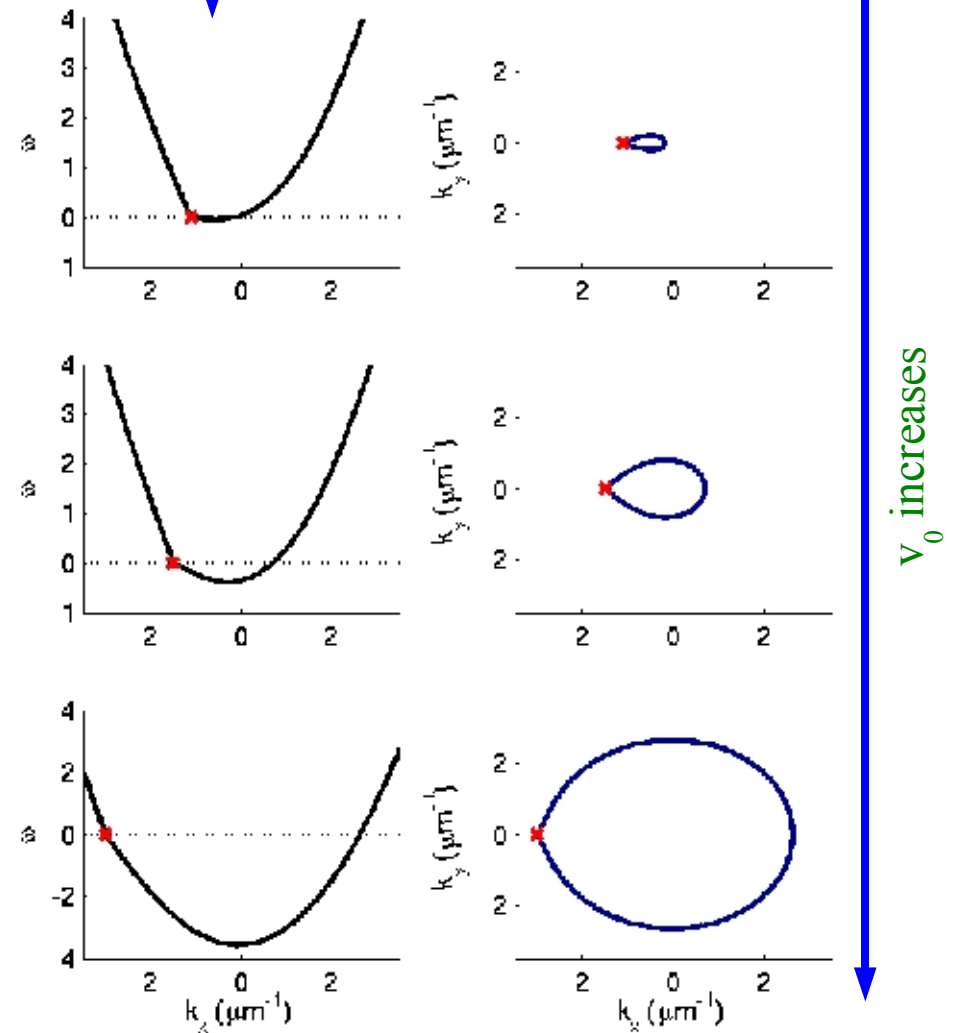
Tilted Bogoliubov dispersion

If  $v_0 < c_s$  ( $c_s$  speed of sound):

- resonance condition **never satisfied**
- **no radiative modes** excited
- perturbation **localized**  
 $\Rightarrow$  **superfluid behaviour**

If  $v_0 > c_s$ :

- a (deformed) **ring of modes** is resonantly excited
- ring **gets wider** for increasing  $v_0$



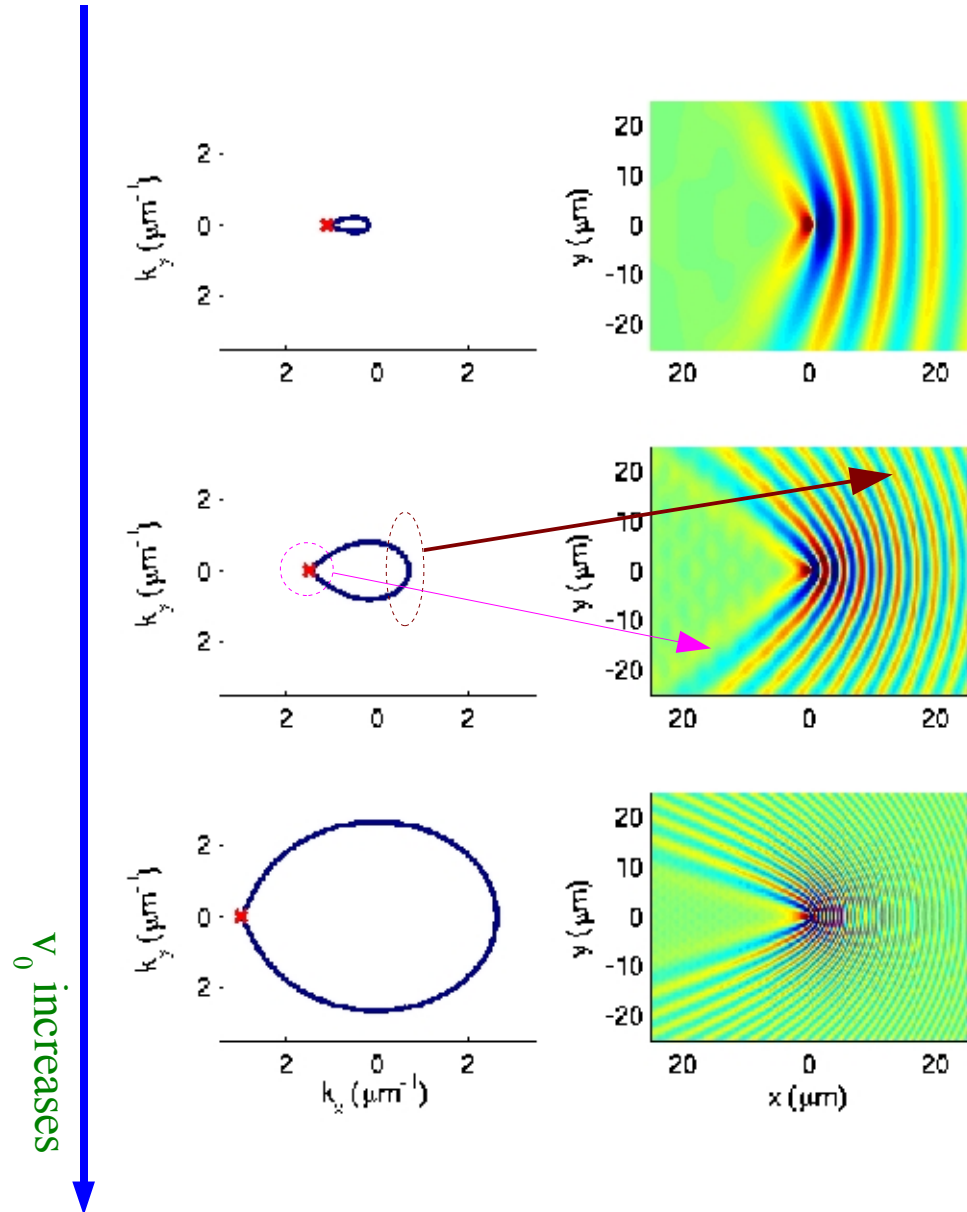
# Theory of Bogoliubov-Cerenkov radiation (III) real space pattern

Each resonantly excited mode:

- propagates from defect along straight line
- propagation velocity:  
group velocity:  $v_g = \nabla_{\mathbf{k}} \omega(\mathbf{k})$   
orthogonal to locus of resonant  $\mathbf{k}$ 's
- interferes with BEC:  
fringes at  $\mathbf{q} = \mathbf{k} - \mathbf{k}_0$

Two regions in spatial pattern:

- Cerenkov cone:  
aperture  $\cos \theta = v_{ph} / v_0$
- Parabolic precursors:  
single-particle scattering on defect



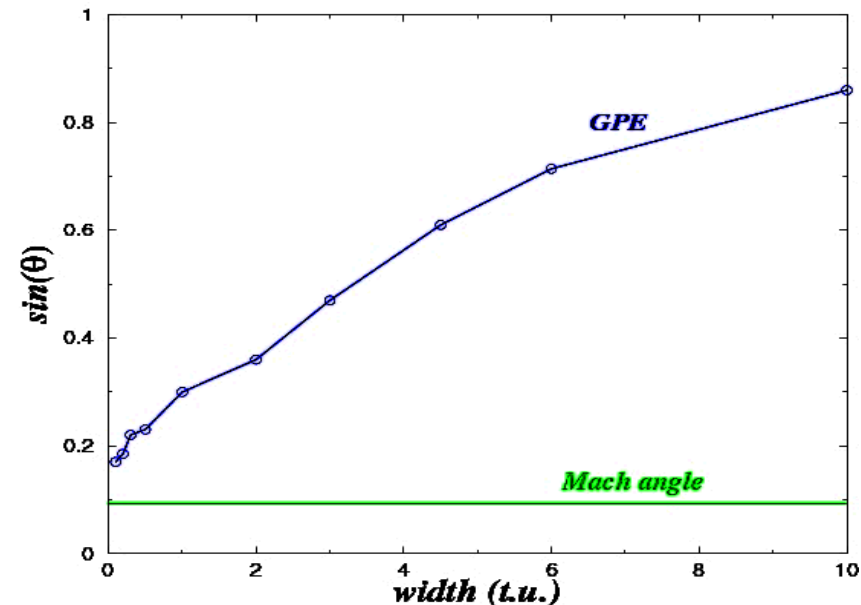
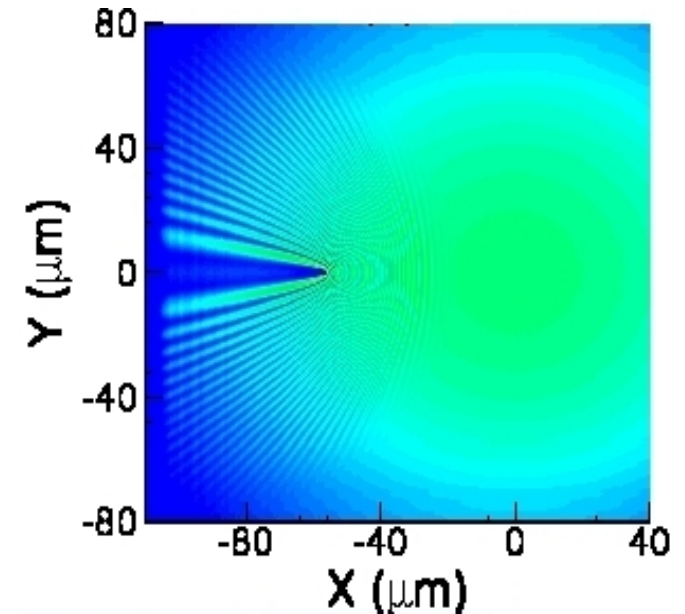
# Comparison with GPE simulations

Pattern qualitatively similar, but in GPE:

- larger aperture of cone
- geometrical shadow behind the defect

Explanation: BEC expansion velocity is not uniform, but rather radial

- Cerenkov angle adds up to geometric shadow angle
- shadow angle decreases for decreasing defect size  $w$
- in small defect limit: Cerenkov angle recovered



Convincing evidence this is Bogoliubov-Cerenkov emission in a quantum fluid !!

# Swimming ducks on a quiet lake



Spatial pattern qualitative similar to Cerenkov effect...  
... is there a connection ??

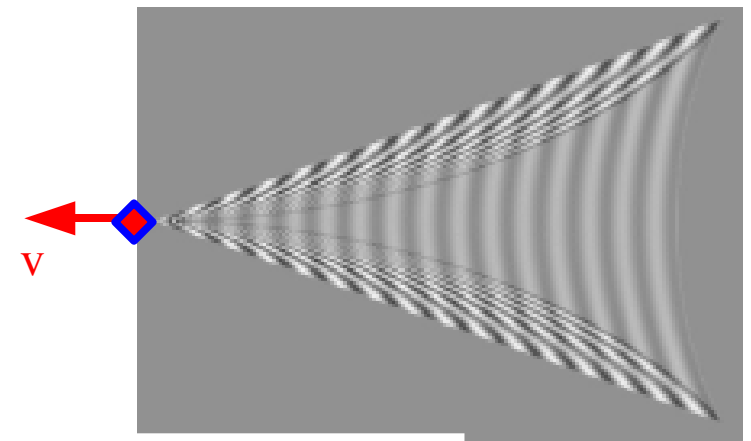
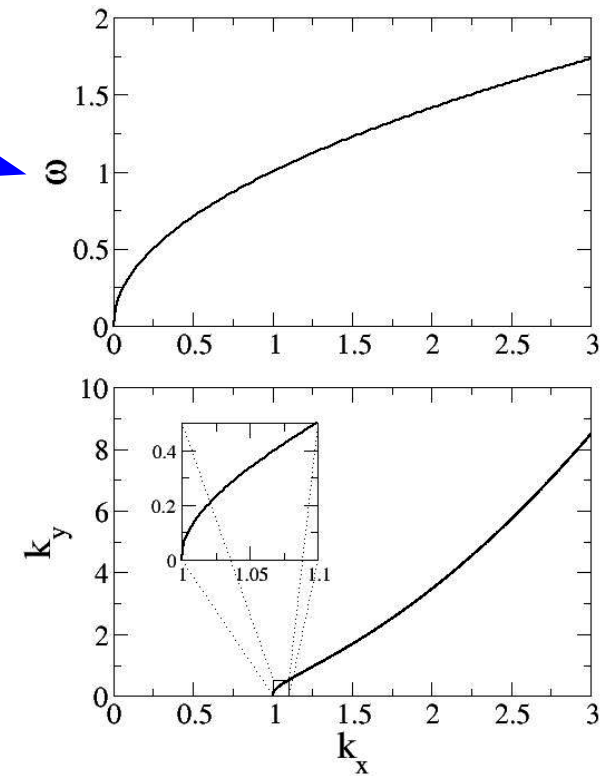
# Cerenkov theory applied to swimming ducks

Surface waves: modelled by **sqrt dispersion law**

Locus of **resonantly excited modes**

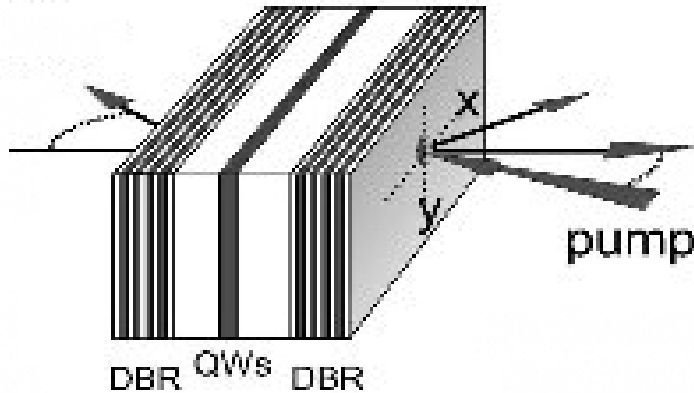
Many interesting **new features**:

- limited range of **group velocity angles**  $\tan \theta_g < 1/\sqrt{8}$ ,  
max value of  $\theta_g$  does **not depend** on  $v$
- for **each position** in space: **two k vectors** available  
⇒ **two intersecting patterns**
- duck **form factor** (of **size  $\sigma$** ) limits range of excited k vectors.  
**Emission suppressed** if  $v^2 \ll g \sigma$ .  
For  $\sigma=20$  cm  $v_{cr}=1.4$  m/s (realistic!!)



see e.g.: G. B. Whitham, *Linear and nonlinear waves* (Wiley, NY, 1974)

# Moving light fluids in planar optical cavities



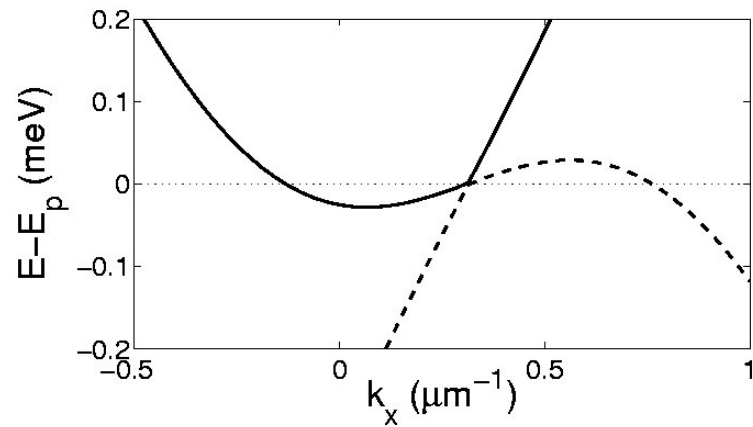
- Photon fluid created by coherent incident laser beam
- Flow speed controlled by incident wavevector  $k_p$
- Photon-photon interactions :  $\chi^{(3)}$  optical nonlinearity, polariton-polariton collisions
- Cavity roughness provides defects

Cerenkov excitation of Bogoliubov modes in moving light fluid

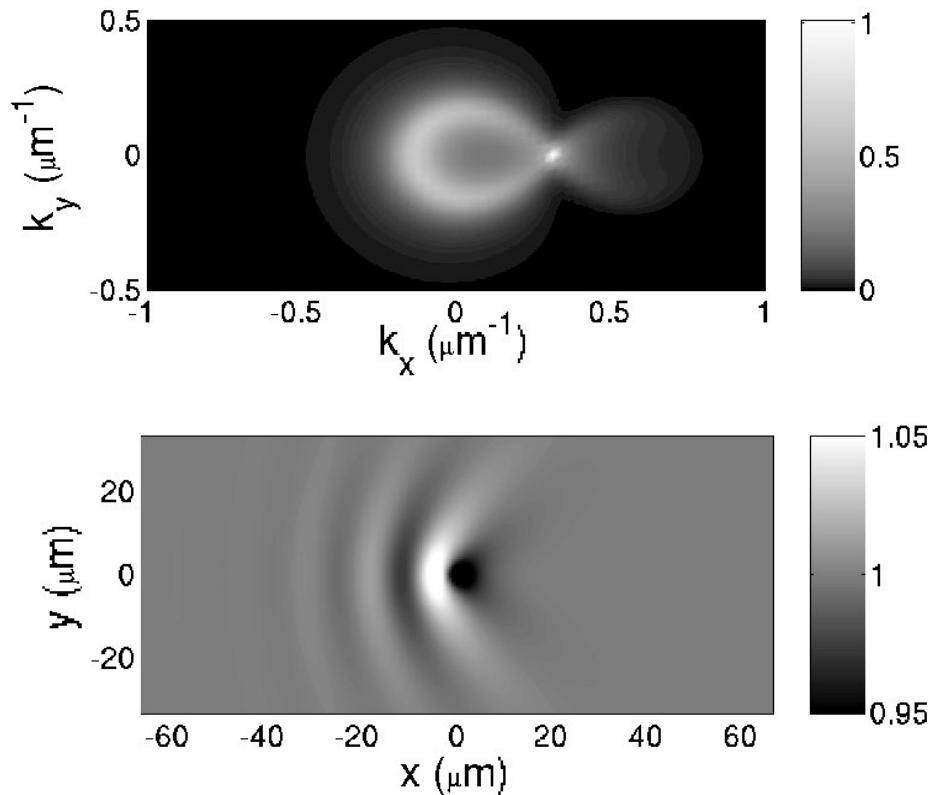
Experimental signal: transmitted and/or reflected light

- far field gives k-space intensity pattern
- near field gives real-space intensity pattern

# Flow against a defect: Cerenkov emission



Incident laser on **resonance** with cavity  
 $\Rightarrow$  **standard Bogoliubov dispersion**



**Cavity damping:**

- **smearing** of k-space pattern
- **spatial decay** of x-space pattern

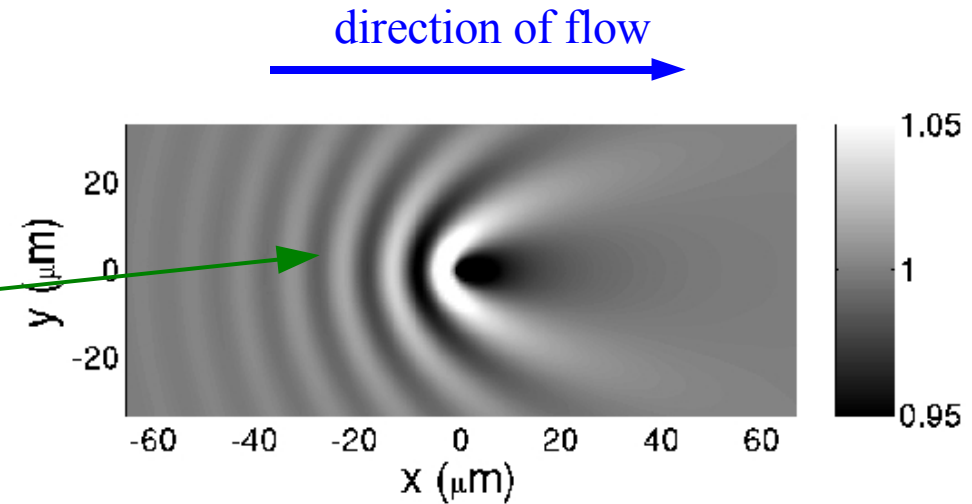
far from defect

# Increasing light intensity: superfluid behaviour

$c_s$  increases with intensity

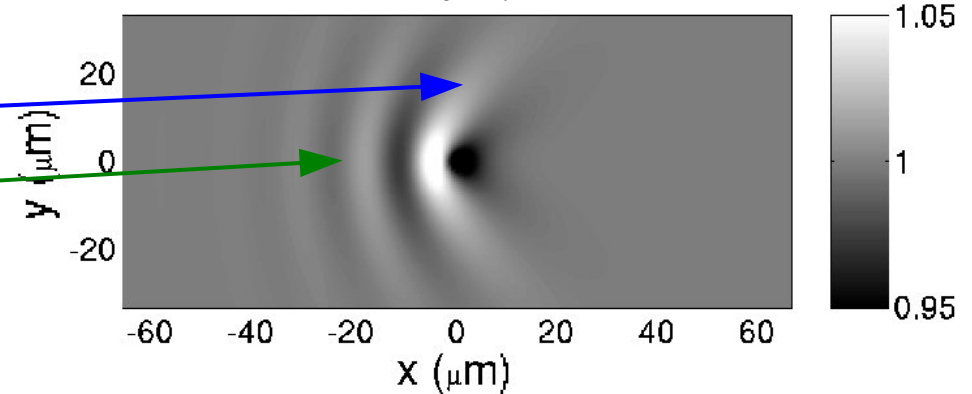
Linear regime  $c_s = 0$

- parabolic wavefronts



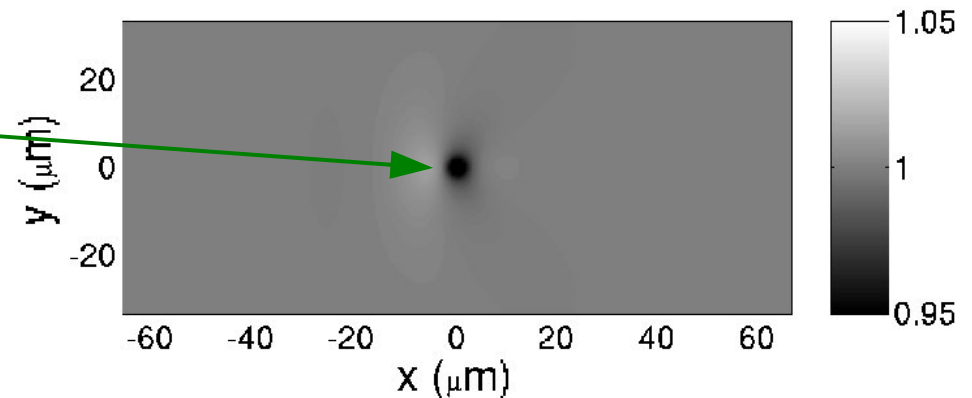
Super-sonic regime  $c_s > v_0$ :

- Cerenkov cone
- parabolic precursors



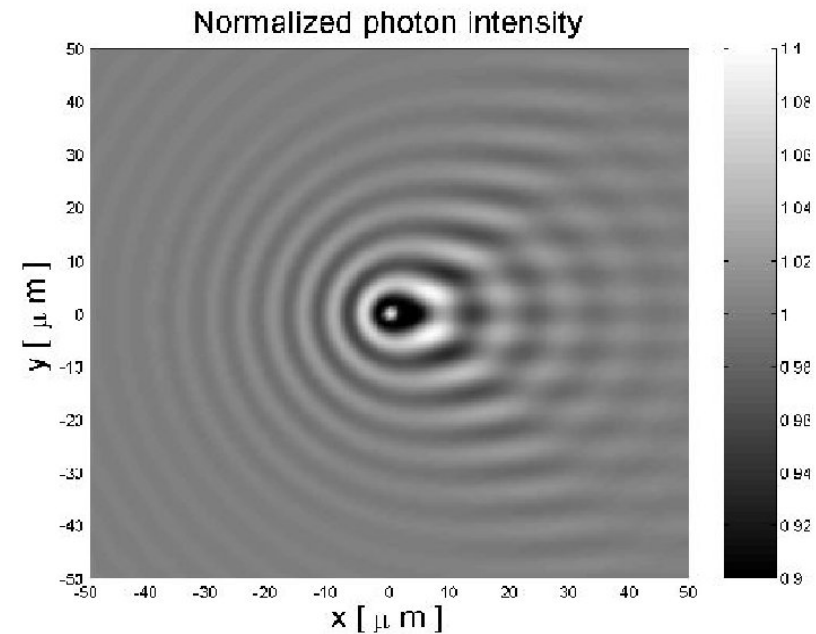
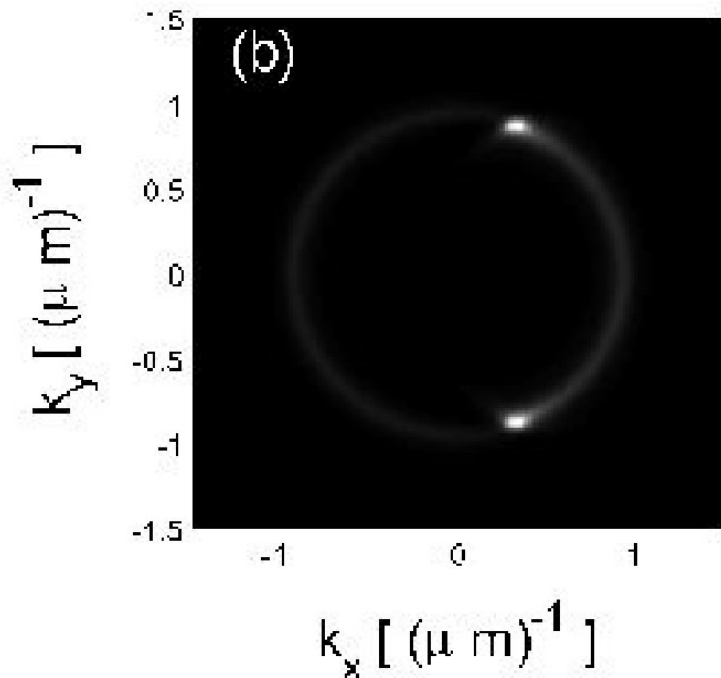
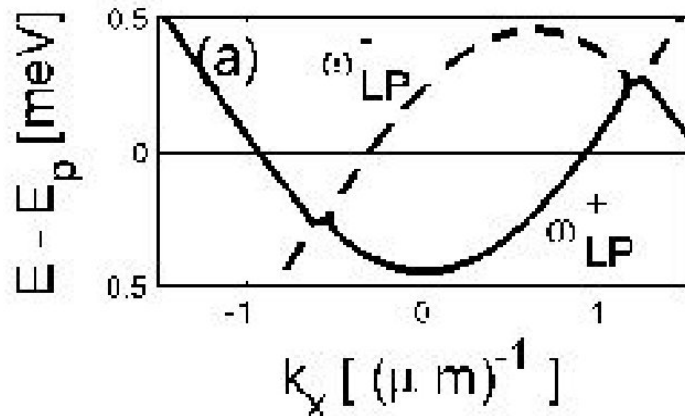
Sub-sonic regime  $c_s < v_0$

- localized perturbation
- polariton superfluid





# Novel features: zebra-Cerenkov effect

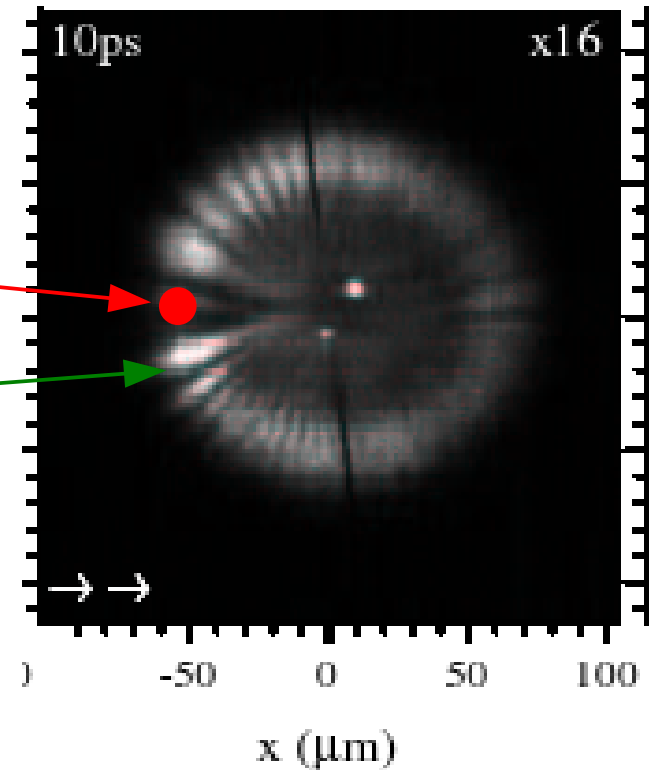


- Concentric rings: usual RRS ring
- Zebra pattern: narrow  $k$ -space peaks, precursor of parametric oscillation
- Many other shapes possible by tuning angle, frequency, intensity ...

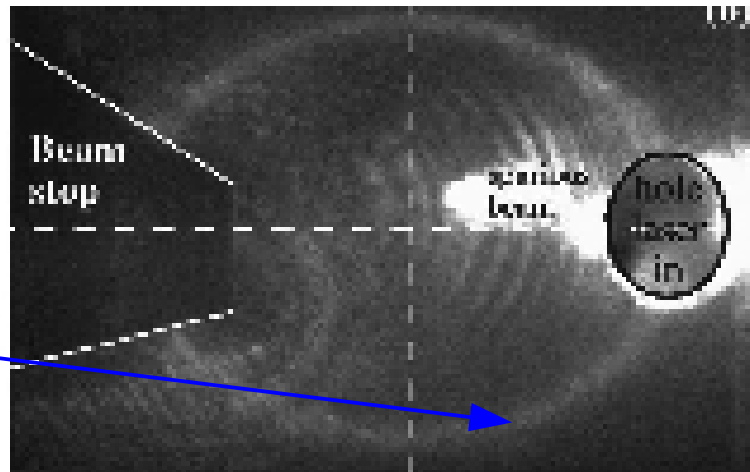
# Preliminary experimental data: linear regime

Polariton cloud expanding against a defect

Real space pattern: fringes



k-space pattern  
Resonant Rayleigh  
scattering ring



Experimental data:

Langbein, 2002 (above)

Houdré, 2000 (below)

# Bogoliubov modes of a non-resonantly pumped polariton Bose-Einstein condensate

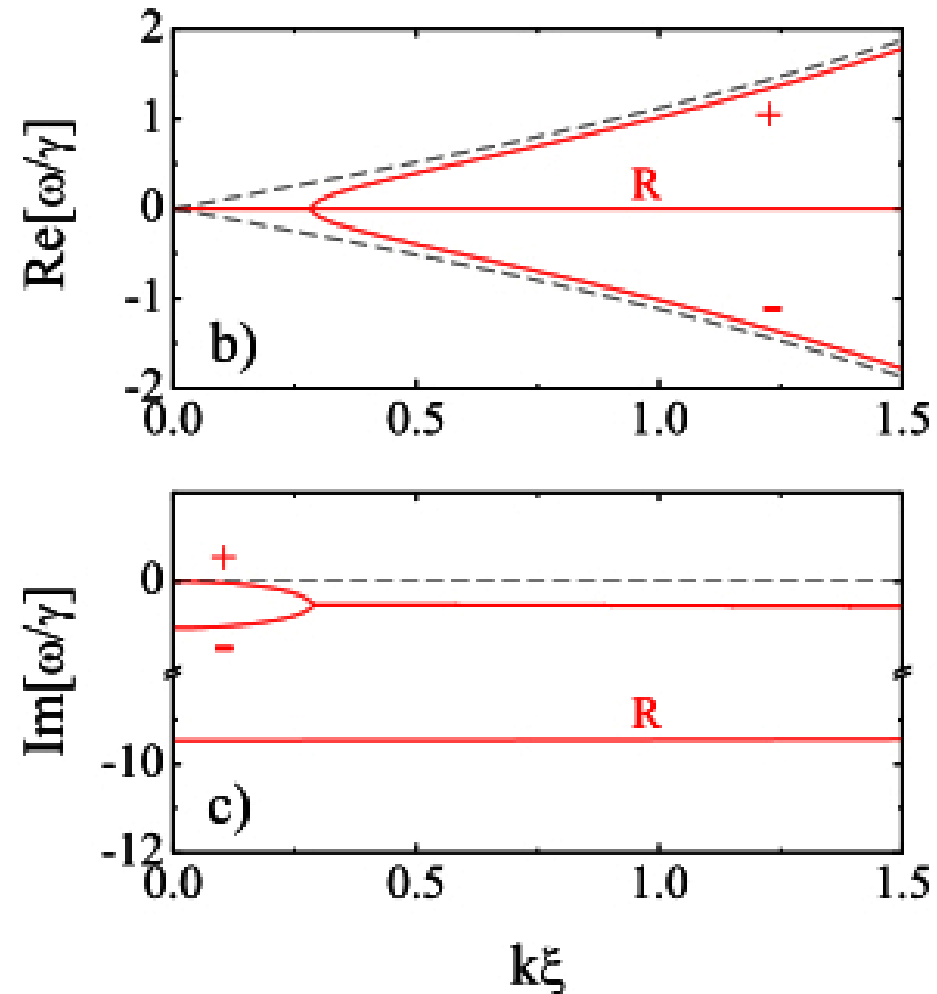
## Linearize non-equilibrium GPE

- Reservoir R mode at  $-i\gamma_R$
- Condensate modes  $\pm$  at:

$$\omega_{\pm}(k) = -\frac{i\Gamma}{2} \pm \sqrt{[\omega_{Bog}(k)]^2 - \frac{\Gamma^2}{4}}$$

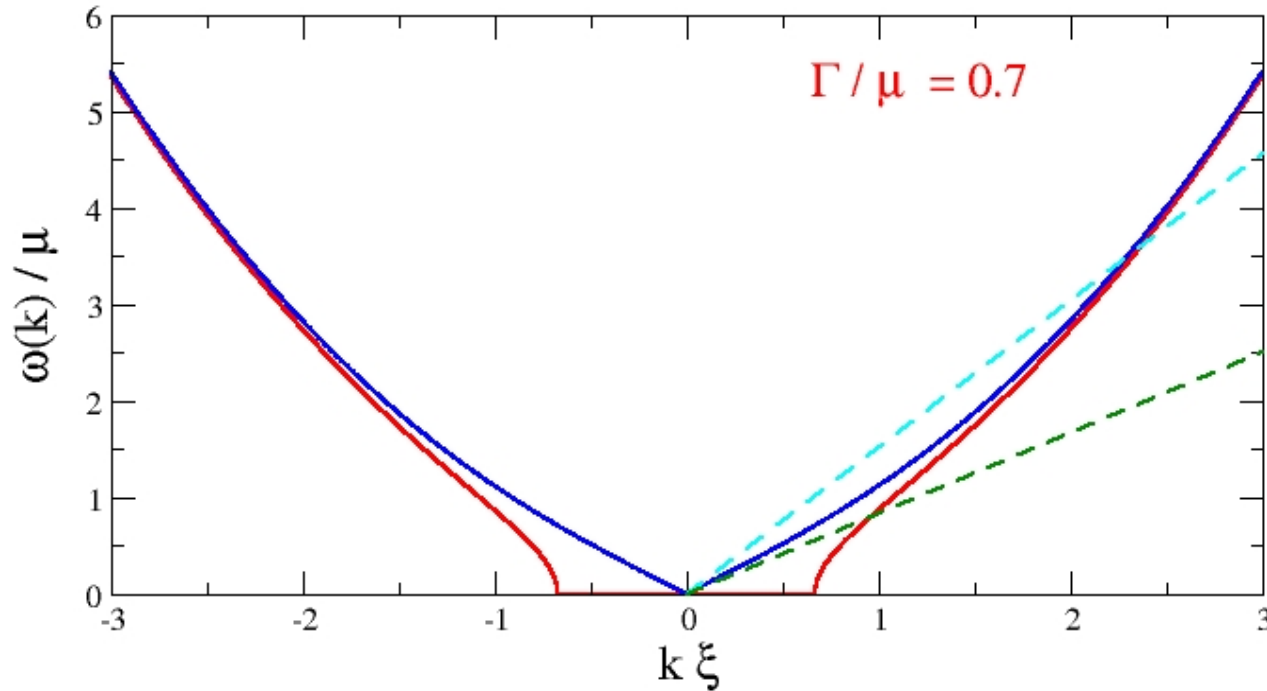
with:

$$\omega_{Bog}(k) = \sqrt{\frac{\hbar k^2}{2m_{LP}} \left( \frac{\hbar k^2}{2m_{LP}} + 2\mu \right)}$$



→ Goldstone sound mode is diffusive !!!

# Consequences on superfluidity of polariton BECs



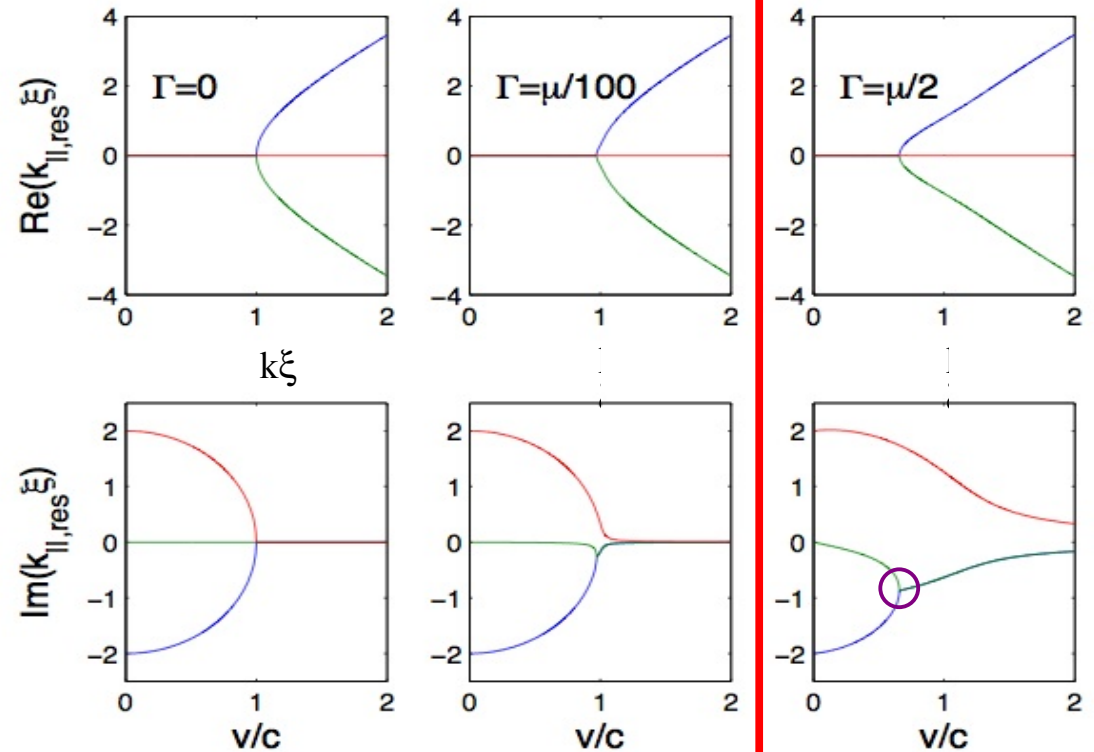
Naïf Cerenkov-Landau argument:

- Landau critical velocity  $v_L = \min_k [\omega(k)/k] = 0$  of non-equilibrium BEC
- Any moving defect expected to emit phonons

# But nature is always richer than expected...

## Low $v$ :

- emitted  $k_{\parallel}$  purely imaginary
- no real propagating phonons
- localized perturbation around defect

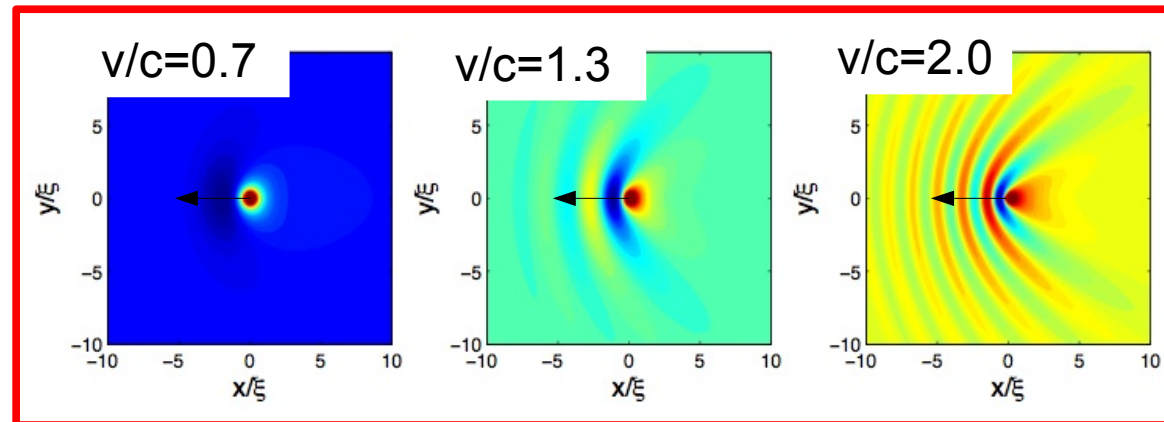


## Critical velocity $v_c < c$ :

- corresponds to bifurcation point
- decreases with  $\Gamma / \mu$

## High $v$ :

- emitted propagating phonons:
  - Cerenkov cone
  - parabolic precursors
- spatial damping of Cerenkov cone



# Conclusions

General description of Cerenkov wave emission by uniformly moving sources and/or in uniform moving media

## A variety of systems to which it can be applied

- **slow light media**: wave vs. group cones  
IC, G.C. La Rocca, M. Artoni, F. Bassani, PRL **87**, 064801 (2001)
- **expanding atomic BEC** against defect potential of blue-detuned laser:  
Bogoliubov-Cerenkov emission of phonons, theory and experiment in agreement  
IC, S.X.Xu, L.A. Collins, and A. Smerzi, PRL **97**, 260403 (2006)
- **swimming ducks** on a quiet lake surface: complex pattern of surface waves  
well-known from hydrodynamics, but still interesting...
- **moving light fluids** in nonlinear planar cavities:  
peculiar dispersion law produces novel Cerenkov patterns  
IC and C.Ciuti, PRL **93**, 166401 (2004), C. Ciuti and IC, Phys. Stat. Sol. (b) **242**, 2224 (2005)
- **polariton condensates**: superfluidity beyond the naive Landau-Cerenkov criterion  
M. Wouters and IC, PRL **99**, 140402 (2007) ; preprint arXiv:0707.1446



**THANKS FOR YOUR**



**ATTENTION !!!**